17 The table gives information about the areas, in hectares, of some farms in Spain.

Area (A hectares)	Frequency
$0 < A \leqslant 20$	40
$20 < A \leqslant 50$	90
$50 < A \leqslant 100$	140
$100 < A \leqslant 300$	140
$300 < A \leqslant 350$	40

On the grid, draw a histogram for this information.



5 9 0 1 2 A 0 1 7

2

Ρ

17

DO NOT WRITE IN THIS AREA



P 5 9 0 1 2 A 0 1 8 2

4

18

19 The curve shown in the diagram has equation

 $y = x^3 - 27x + k$ where k is a positive constant with k < 54

The curve has a maximum point at A(a, b)The curve has a minimum point at B(c, d)



Diagram **NOT** accurately drawn

Using differentiation, find the value of b - dShow your working clearly.



Turn over 🕨

 $20\,$ Two functions, f and g are defined as

$$f: x \mapsto 1 + \frac{1}{x}$$
 for $x > 0$

$$g: x \mapsto \frac{x+1}{2}$$
 for $x > 0$

Given that h = fg

express the inverse function h^{-1} in the form $h^{-1}: x \mapsto \dots$

 $h^{-1}: x \mapsto$

(Total for Question 20 is 4 marks)



21 (a) Show that $x(x - 1)(x + 1) = x^3 - x$

(b) Prove that the difference between a whole number and the cube of this number is always a multiple of 6

(3)

(1)

(Total for Question 21 is 4 marks)



22 A 3-D shape consists of a hollow sphere made of metal.



The diagram shows a cross section drawn through the centre, O, of the sphere.



Image: Second system
Image: Se

Diagram **NOT** accurately drawn

The internal radius of the sphere is 1.2 m. The thickness of the metal is *t* cm.

The density of the metal is 2700 kg per m³

The mass of the 3-D shape is 1980kg.

Work out the value of *t*. Give your answer correct to 2 significant figures. DO NOT WRITE IN THIS AREA

(Total for Question 22 is 5 marks)

t =

23 Work out the sum of the multiples of 3 between 1 and 1000

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

(Total for Question 23 is 4 marks)

TOTAL FOR PAPER IS 100 MARKS

