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Mark Scheme (Standardisation)

January 2020

Pearson Edexcel International GCSE Mathematics A (4MA1) Paper 2H

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded.
 Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
 - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

Types of mark

- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- SC special case
- o oe or equivalent (and appropriate)

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- o dep dependent
- o indep independent
- o awrt answer which rounds to
- eeoo each error or omission

No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If there is a choice of methods shown, mark the method that leads to the answer on the answer line; where no answer is given on the answer line, award the lowest mark from the methods shown.

If there is no answer on the answer line then check the working for an obvious answer.

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

International GCSE Maths

Apart from Questions 3, 7b, 12, 17, 20, 22 the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method

| | Q | Working | Answer | Mark | Notes |
|---|-----|---|--------|------|---|
| 1 | (a) | | x^7 | 1 | B1 |
| | (b) | eg $7^8 \times 7^4 = 7^{12}$ or $7^8 \div 7^3 = 7^5$ or $7^5 \times 7^4$ or $7^4 \div 7^3$ = 7 or $7^8 \times 7$ or $7^{12} \div 7^3 = 7^{12} - 3$ | | 2 | M1 for one correct step – must be written as a power of 7 |
| | | | 7^9 | | A1 for 7 ⁹ |
| | | | | | Total 3 marks |

| 2 | 32.4×100^3 | | 2 | M1 | for 32.4×100^3 oe |
|---|---------------------|------------|---|----|--|
| | | 32 400 000 | | A1 | for 32 400 000 accept 3.24×10^7 |
| | | | | | Total 2 marks |

| $\frac{3}{3}$ $\frac{14}{3}(+)\frac{19}{5}$ or $(4)\frac{10}{15}(+)(3)\frac{12}{15}$ or $(4)\frac{10a}{15a}(+)(3)\frac{12a}{15a}$ | | 3 | M1 | for correct improper fractions or fractional part of numbers written correctly over a common denominator |
|---|-------|---|----|--|
| $eg \frac{14 \times 5 + 19 \times 3}{3 \times 5} \text{ or } \frac{70}{15} + \frac{57}{15} \text{ or } \frac{70a}{15a} + \frac{57a}{15a} \text{ or}$ $4\frac{10}{15} + 3\frac{12}{15} = 7\frac{22}{15} \text{ oe}$ | | | M1 | for correct fractions with a common denominator of 15 or a multiple of 15 |
| $\frac{70}{15} + \frac{57}{15} = \frac{127}{15} = 8\frac{7}{15} \text{ or } 7\frac{22}{15} = 8\frac{7}{15}$ or if shows $8\frac{7}{15} = \frac{127}{15}$ at the beginning then show that the addition comes to $\frac{127}{15}$ | Shown | | A1 | dep on M2 for a correct answer from fully correct working or shows that $RHS = \frac{127}{15} \text{ and fully correct working}$ $shows LHS = \frac{127}{15}$ |
| | | | | Total 3 marks |

| 4 | 30 + 4x + 10 + x + 20 (= $5x + 60$) or $180 - 30 $ (=150) | | 4 | M1 | Allow $5x + 60 = n$ where $n \neq 180$ or for subtracting 30 from 180 | M2 for $5x + 30 = 150$ oe |
|---|---|----|---|----|--|---------------------------|
| | e.g. $30 + 4x + 10 + x + 20 = 180$ or $5x + 60 = 180$ oe or $180 - 30 - 10 - 20$ (=120) | | | M1 | for setting up the equation or for subtracting all numerical values of angles from 180 | |
| | 5x = 120 or 120 ÷ 5 | | | M1 | for correctly simplifying dividing '120' by 5 | to $ax = b$ or for |
| | | 24 | | A1 | for 24 | Total 4 marks |

| 5 | Fully correct angle | 2 | B2 | Fully correct angle bisector with all |
|---|---------------------|---|----|---------------------------------------|
| | bisector with all | | | arcs shown. |
| | relevant arcs | | | B1 for all arcs and no angle bisector |
| | shown | | | drawn or for a correct angle bisector |
| | | | | within guidelines but not arcs or |
| | | | | insufficient arcs |
| | | | | Total 2 marks |

| 6 | 1 - (0.24 + 0.31) (= 0.45) | 4 | M1 | or for a correct equation for |
|---|-----------------------------------|----|----|---------------------------------------|
| | Or | | | missing values eg |
| | $(0.24 + 0.31) \times 180 (= 99)$ | | | x + 0.24 + 2x + 0.31 = 1 oe |
| | | | | (can be implied by 2 probabilities |
| | | | | that total 0.45 in table if not |
| | | | | contradicted in working space) |
| | '0.45' ÷ 3 (= 0.15) | | M1 | (or 0.15 correctly placed in table |
| | Or | | | as long as not contradicted) |
| | '0.45' × 180 (= 81) | | | |
| | Or | | | |
| | 180 – 99 (= 81) | | | |
| | '0.15' × 180 | | M1 | or for an answer of $\frac{27}{}$ |
| | Or | | | or for an answer of $\frac{180}{180}$ |
| | '81' ÷ 3 | | | |
| | | 27 | A1 | |
| | | | | Total 4 marks |

| 7 | (a) | 2x > 4 - 7 or x | + 3.5 > 2 | | 2 | M1 | For a correct first step allow $2x = 4 - 7$ or $x + 3.5 = 2$ or an answer of $x = -1.5$ or $x < -1.5$ or $x < -1.5$ |
|---|-----|----------------------|--|----------|---|----|--|
| | | | | x > -1.5 | | A1 | for $x > -1.5$ oe |
| | (b) | $(x \pm 8)(x \pm 5)$ | $\frac{-(-3) \pm \sqrt{(-3)^2 - 4 \times 1 \times (-40)}}{2 \times 1}$ or $\frac{3 \pm \sqrt{9 + 160}}{2}$ | | | M1 | or $(x + a)(x + b)$ where $ab = -40$ or $a + b = -5$ OR correct substitution into quadratic formula (condone one sign error in a , b or c and missing brackets) (if + rather than \pm shown then award M1 only unless recovered with answers) |
| | | (x-8)(x+5) | $\frac{3\pm\sqrt{169}}{2}$ or $\frac{3\pm13}{2}$ | | | M1 | $\frac{3 \pm \sqrt{169}}{2}$ or $\frac{3 \pm 13}{2}$ |
| | | | | 8, -5 | 3 | A1 | dep on at least M1 for correct values |
| | | | | | | | Total 5 marks |

| 8 (a) | 545 - 500 (= 45) or $592 - 545 (= 47)$ | | 4 | M1 | may be seen as part of a calcul- | ation |
|--------------|--|----------------------------|---|----|---|--|
| | $\frac{45}{500} \times 100 (=9) \text{ or } \frac{47}{545} \times 100 (=8.6)$ | | | M1 | for one correct expression (allocorrect expression for 8.6 through | |
| | $\frac{45}{500} \times 100 (=9)$ and $\frac{47}{545} \times 100 (=8.6)$ | | | M1 | for both correct expressions or finds 109% of 545: 1.09 × 545: 545 (49.05) or having found "8 500: 1.086 × 500(=543) or 8.60 | (=594.05) or 9% of 8.6%" finds 108.6% of |
| | | No, 9(%) and 8.6(%) | | A1 | for no oe, 9% and 8.6% seen of no oe and 9% and 594.05 or 8. No, 49.05 > 45 or No 594.05 > | 6% and 543 or |
| Alternative | e mark scheme for 8(a) | | | | | |
| | $\frac{545}{500} \times 100(=109) \text{ or } \frac{545}{500}(=1.09) \text{ or}$ $\frac{592}{545} \times 100(=108.6) \text{ or } \frac{592}{545}(=1.086)$ $\frac{545}{500} \times 100(=109) \text{ or } \frac{545}{500}(=1.09) \text{ and}$ $\frac{592}{545} \times 100(=108.6) \text{ or } \frac{592}{545}(=1.086)$ | | 4 | M3 | for both correct expressions what 109 or 1.09 and 108.6 or 1.086 (allow 108 or 108.7 from correct or 1.08 or 1.087 from correct with throughout) (if not M3 then award M2 for expressions) | oct working for 108.6 working for 1.086 |
| | 343 343 | No, 109(%) and 108.6(%) | | A1 | oe eg no and 1.09 and 1.086 | |
| (b) | 952 ÷ 85 × 100 oe (=1120) | | 3 | M1 | for a method to find price before discount | M2 for $\frac{952}{85} \times 15$ |
| | 0.15 × "1120" or "1120" – 952 oe | | | M1 | for a correct method to find discount | |
| | | 168 | | A1 | | |
| | | | | | | Total 7 marks |

| 9 | 19.3 × 150 | | 2 | M1 | for 19.3 × 150 |
|---|------------|------|---|----|----------------|
| | | 2895 | | A1 | for 2895 |
| | | | | | Total 2 marks |

| 10 | $50 \times 60 \ (= 3000) \text{ or } 50 \div 1000 \ (= 0.05 \text{ or } \frac{1}{20})$ | | 3 | M1 | for 50 with at least one of \div 1000 or \times 60 |
|----|--|-----|---|----|--|
| | or 50 × 60 × 60 (= 180 000) or | | | | or |
| | $\frac{60 \times 60}{1000} (= 3.6)$ | | | | $\frac{60 \times 60}{1000} (=3.6)$ |
| | or | | | | or |
| | $1000 \div 60 \div 60 = 0.27777 \text{ or } \frac{5}{18}$ | | | | $1000 \div 60 \div 60$ |
| | $50 \times \frac{60 \times 60}{1000}$ oe eg $50 \div \frac{5}{18}$ | | | M1 | (dep) for a complete method |
| | | 180 | | A1 | for 180 (SCB1 for both conversion factors correct but applying them wrongly $eg \; \frac{50 \times 1000}{60 \times 60})$ |
| | | | | | Total 3 marks |

| _ | _ _ | | 1 | | |
|----------------|---|------|---|----|---|
| 11 | $(AC^2 =) 17^2 - 15^2$ | | 5 | M1 | |
| | $(AC =) \sqrt{17^2 - 15^2} \ (= \sqrt{64} = 8)$ | | | M1 | |
| | $\frac{\pi \times '8'}{2} (= 4\pi = 12.566)$ | | | M1 | dep on M2 for $\frac{\pi \times '8'}{2}$ oe or 4π |
| | '12.566'+ 15 + 17 | | | M1 | 12.5663 for '12.566' + 15 + 17 and no additional values |
| | | 44.6 | | A1 | for awrt 44.6 |
| | | | | | Total 5 marks |
| Alternative ma | ark scheme for 11 | • | | | |
| | $\cos^{-1}\left(\frac{15}{17}\right) (= 28.0724) \text{ or } \sin^{-1}\left(\frac{15}{17}\right) (= 61.9275)$ | | 5 | M1 | for a correct method to find one of the angles |
| | $15 \times \tan (28.0724) (= 8) \text{ or } 15 \div \tan (61.9275) (= 8)$ | | | M1 | |
| | $\frac{\pi \times '8'}{2} \ (= 4\pi = 12.566)$ | | | M1 | dep on M2 for $\frac{\pi \times '8'}{2}$ or 12.5663 or 4π |
| | "12.566" + 15 + 17 | | | M1 | for "12.566" + 15 + 17 and no additional values |
| | | 44.6 | | A1 | for awrt 44.6 |
| | | | | | Total 5 marks |

| 12 | Litres per amount of money and then conversion | | |
|----|---|---------------------------------|---|
| | $\frac{8.6 \times 10^5}{770000} (=1.1168) l/\$$ | | M1 Number of litres per \$ for D |
| | $\frac{4.2 \times 10^5}{2500000} (=0.168) l/k$ | | M1 Number of litres per Krone for A |
| | A: l/\$ to l/k '1.1168' ÷ 6.57 (= 0.1699)or D: l/k to l/\$ '0.168' × 6.57 (= 1.103) | | M1 <i>l</i> /\$ to <i>l</i> /k for A or <i>l</i> /k to <i>l</i> /\$ for D |
| | | Arctic Oil and relevant figures | A1 for Arctic Oil with 1.1168 and 1.10376 or 0.168 and 0.1699 |
| | Conversion then litres per amount of money | | |
| | $\frac{2500000}{6.57}$ (=380517.5) or 770 000 × 6.57(= 505 8900) | | M1 Changing Krone to \$ or \$ to Krone |
| | $\frac{4.2 \times 10^5}{2500000}$ (=0.168) or $\frac{4.2 \times 10^5}{'380517.5'}$ (=1.103) | | M1 Litres per Krone or litres per \$ for D |
| | $\frac{8.6 \times 10^5}{770000}$ (=1.1168) or $\frac{8.6 \times 10^5}{5058900}$ (=0.1699) | | M1 Litres per Krone or litres per \$ for A |
| | | Arctic Oil and | A1 for Arctic Oil with 1.1168 and |
| | | relevant figures | 1.10376 or 0.168 and 0.1699 |
| | Cost per litre then conversion | | |
| | $\frac{2500000}{4.2\times10^5}(=5.952)$ | | M1 Price per litre in Krone for D |
| | $\frac{770000}{8.6 \times 10^5} (0.895)$ | | M1 Price per litre in \$ for A |
| | '5.952' ÷ 6.57(=0.9059) or '0.895' × 6.57(= 5.882) | | M1 Conversion of Krone to \$ or \$ to Krone |
| | | Arctic Oil and relevant figures | A1 For Arctic Oil with 5.952 and 5.882 or 0.895 and 0.9059 |

| | Conversion then cost per lit | tre | | | |
|---------|---|---|---------------------------------|------------|--|
| | $\frac{2500000}{6.57}$ (=380517.5) or 77 | 70 000 × 6.57(= 505 8900) | | M1 | Changing Krone to \$ or \$ to Krone |
| | $\frac{2500000}{4.2\times10^5}$ (= 5.952) or $\frac{'3805}{4.2\times10^5}$ | $\frac{17.5'}{\times 10^5}$ (=0.9059) | | M1 | Cost per litre in Krone or cost per litre in \$ for D |
| | $\frac{770000}{8.6 \times 10^5} (= 0.895)$ or $\frac{'5058}{8.6 \times 10^5}$ | $\frac{8900'}{\langle 10^5} (=5.882)$ | | M1 | Cost per litre in \$ or cost per litre in Krone for A |
| | | | Arctic Oil and relevant figures | A1 | For Arctic Oil with 5.952 and 5.882 or 0.895 and 0.9059 |
| | Comparing equal amounts | | | | |
| | $\frac{8.6 \times 10^5}{4.2 \times 10^5} (= \frac{43}{21} = 2.047)$ | $\frac{4.2 \times 10^5}{8.6 \times 10^5} (= \frac{21}{43} = 0.488)$ | | M1 | Multiplier for same amount of D as A or same amount of A as D |
| | '2.047'×2500 000 K (=5119047.619)K | '2.047' × 770 000 \$ (=376046.511)\$ | | M1 | Cost of equal amount of D as A or A as D |
| | '5119047.619'÷6.57 = 779154.88\$ or 770 000×6.57=5058900 K | '376046.511'× 6.57 =2470625.58K or 2500 000÷6.57 = 380517\$ | | M1 | Converts so can compare costs – either K to \$ or original A to K or \$ to K or original D to \$ |
| | | | Arctic Oil and relevant figures | A1 | Arctic Oil and 779154 or with 2470625(figures may be rounded) |
| | | | | | Or Arctic Oil with 5119047 and 5058900 or with 376046 and 380517 |
| Student | s may compare other equal am | ounts – please use the scheme t | hat best fits their met | thod and a | ward marks appropriately. |
| | | | | | Total 4 marks |

| | at the <u>circumference</u> (or <u>on the circle)</u> | | | | |
|----|--|-----|---|----|-----------------------------------|
| | angles subtended by the same arc(or chord) | | | | |
| | alternate segment theorem | | | | |
| | angle between tangent and radius (diameter) | | | | |
| | angles at a point opposite angles in a cyclic quadrilateral | | | | |
| | opposite) | | | | |
| | vertically <u>opposite angles</u> (or <u>vertically</u> | | | | |
| | <u>alternate</u> angles | | | | |
| | <u>isosceles</u> triangle | | | | |
| | triangle | | | | reason) |
| | angles in a triangle add up to 180°/angles in a | | | | M1) for a correct circle theorem |
| | is double angle at circumference oe) | | | | (if not B2 then award B1(dep on |
| | angle in a semicircle is 90° (or angle at centre | | | B2 | for their method used |
| | Angles in the same segment are equal, | | | B2 | Dep on M1 for all correct reasons |
| | aligic ACD = 90 of aligic ADD = 90 | 30° | | A1 | For a correct answer of 30 |
| 13 | Angle $CAD = 28^{\circ}$ or angle $ACB = 32^{\circ}$ or angle $ACD = 90^{\circ}$ or angle $ABD = 90^{\circ}$ | | 4 | M1 | |

| 14 (a) | | | 2 | | for $\frac{13}{20}$ and $\frac{7}{20}$ on the first branch (0.65 and 0.35) |
|---------------|--|---|---|----|---|
| | | Correct probabilities on the tree diagram | | B1 | for $\frac{12}{19}$, $\frac{7}{19}$, $\frac{13}{19}$ and $\frac{6}{19}$ on the second branch (accept 2 dp or better 0.6315, 0.3684, 0.6842, 0.3157) |
| (b) | $\frac{7}{20} \times \frac{6}{19}$ oe only | | 2 | M1 | ft from (a) as long as probabilities less than 1 |
| | $\frac{21}{190}$ | 21 190 | | A1 | for $\frac{21}{190}$ oe or 0.11 (at least 2 dp) |
| | | | | | Total 4 marks |
| | | | | | |

| 15 | C, B, E | 3 | B3 | for all 3 correct | |
|----|---------|---|-----|-------------------|---------------|
| | | | (B2 | for 2 correct) | |
| | | | (B1 | for 1 correct) | |
| | | | | - | Total 3 marks |

| 16 | $y^2 = \frac{x+1}{x-4}$ | | 4 | M1 | for squaring |
|----|--|--------------------------------|---|----|---|
| | $y^{2}(x-4) = x+1$ or $y^{2}x-4y^{2} = x+1$ | | | M1 | for removing the fraction |
| | $y^2x - x = 4y^2 + 1$ or $-4y^2 - 1 = x - y^2x$ or $x(y^2 - 1) = 4y^2 + 1$ or $-4y^2 - 1 = x(1 - y^2)$ | | | M1 | for expanding the bracket and rearranging for <i>x</i> so that the terms in <i>x</i> are on one side of the correct equation |
| | | $x = \frac{4y^2 + 1}{y^2 - 1}$ | | A1 | for $x = \frac{4y^2 + 1}{y^2 - 1}$ or $x = \frac{-4y^2 - 1}{1 - y^2}$ |
| | | | | | (need to see $x =$ somewhere) |
| | | | | | Total 4 marks |

| 17 | e.g. $n^2 - (n-1)^2$ or $(n+1)^2 - n^2$ | | 3 | M1 | for setting up a correct algebraic expression (any letter can be used) |
|----|---|-----------------------------|---|----|---|
| | e.g. $n^2 - n^2 + 2n - 1$ or $n^2 + 2n + 1 - n^2$ | | | M1 | Correct expansion of brackets and correct signs or a correct result |
| | | e.g. $2n - 1$ is always odd | | A1 | dep on M2 for eg $2n - 1$ or $2n + 1$ or $-(2n + 1)$ oe and a suitable conclusion SCB1 for eg $(2n)^2 - (2n - 1)^2$ or $(2n + 1)^2 - (2n)^2$ oe |
| | | | | | Total 3 marks |

| 18 (a) | $(0.7 \times 10) + (3.4 \times 5) + (1 \times 9) + (2.5 \times 6) + (4.8 \times 15)$ = 7 + 17 + 9 + 15 + 72 (= 120) no. of sml squares = $(10 \times 7) + (5 \times 34) + (9 \times 10) + (6 \times 25) + (15 \times 48)$ = 70 + 170 + 90 + 150 + 720 (= 1200) or all correct values in bars oe not added | | 3 | M1 | for a correct method to work out the total area eg total frequency or number of small squares or other correct method (allow one error in method) [count use of 25 for 24 as one error] or all correct values in bars oe not added |
|---------------|---|------------------|---|----|---|
| | $(1 \times 7) + (2.5 \times 6) + (5 \times 4.8) = 7 + 15 + 24 (= 46)$ or no. of sml squares $(48 \times 5) + (6 \times 25) + (7 \times 10) = 240 + 150 + 70 (= 460)$ | | | M1 | for a correct method to work out the area between 17 minutes and 35 minutes eg using frequency density or number of small squares oe |
| | $\frac{46}{120}$ | $\frac{46}{120}$ | | A1 | for $\frac{46}{120}$ oe (allow 2 dp or better 0.3833 or 38% or better) |
| (b) | | | 2 | M1 | for $\frac{n}{15}$ where $n < 15$ or $\frac{q}{720}$ where $q < 720$ or $\frac{r}{72}$ where $r < 72$ or $\frac{9}{m}$ where $m > 9$ or $\frac{432}{p}$ where $p > 432$ $\frac{43.2}{t}$ where $t > 43.2$ |
| | | $\frac{9}{15}$ | | A1 | $\frac{9}{15}$ oe |
| | | | | | Total 5 marks |

| 19 (a) | | y = Ax + b(ca) | 1 | D1 | for A |
|--------|--|-----------------------|---|------|--|
| 19 (a) | | y = -4x + k (oe) | 1 | B1 | for $y = -4x$ or $y = -4x + k$ where k is any numerical value $k \ne 7$ |
| | | | | | · · |
| | | | | | Could be written in another form e.g. $3y + 12x = 20$ |
| (1-) | 2 1 1 2 2 | | 4 | 3.61 | |
| (b) | $m = \frac{-2-1}{23}$ or $m = \frac{12}{-3-2}$ or $-\frac{3}{5}$ or -0.6 | | 4 | M1 | for using $m = \frac{y_2 - y_1}{x_2 - x_1}$ |
| | $m_p = \frac{5}{3}$ | | | M1ft | for using $m_1 \times m_2 = -1$ |
| | $4 = \frac{5}{3}(-6) + c$ oe eg $4 = -10 + c$ $(c = 14)$ | | | M1ft | dep on previous M1 for substituting (-6, 4) into linear equation formula |
| | $y-4=\frac{5}{3}(x6)$ | | | | $4 = \frac{5}{3}x + c \text{ to find value of } c \text{ or}$ |
| | | | | | $y = \frac{5}{3}x + 14$ or $y = 1.66x + 14$ |
| | | Eg $5x - 3y + 42 = 0$ | | A1 | for correct simplified equation where all |
| | | 5x - 3y + 42 = 0 | | | values are integers |
| | | | | | 10x - 6y + 84 = 0 or |
| | | | | | 3y = 5x + 42 oe |
| | | | | | Total 5 marks |

| 20 | $\frac{18}{\sqrt{7}+1} \times \frac{\sqrt{7}-1}{\sqrt{7}-1}$ | | 3 | $ \text{for } \frac{18}{\sqrt{7}+1} \times \frac{\sqrt{7}-1}{\sqrt{7}-1} $ |
|----|--|---------------|---|---|
| | eg $\frac{18(\sqrt{7}-1)}{7-1}$ | | | M1 Dep on M1 for a correct numerator and multiplying out the denominator to 7 – 1 or 6 |
| | $3\sqrt{7}-3$ | $3\sqrt{7}-3$ | | A1 Dep on M2 Allow $3\sqrt{7}-1$ |
| | | | | Total 3 marks |

| 21 | (a)(i) | | (0, 6) | 2 | B1 | |
|----|--------|---|--|---|----|--|
| | (iii) | | (2, 6) | | B1 | |
| | (b) | eg $(x-4)^2 + 3(x-4) + 4$ oe or eg $(x+\frac{3}{2}-4)^2 - \frac{9}{4} + 4$ oe or eg $x^2 + 3x + 10$ oe or eg $(x+\frac{3}{2})^2 - \frac{9}{4} + 4 + 6$ oe eg $y - 6 = x^2 + 3x + 4$ | | 2 | M1 | for applying one of the transformations to the equation |
| | | | $y = (x-4)^{2} + 3(x-4) + 10$ or $y = (x + \frac{3}{2} - 4)^{2} - \frac{9}{4} + 4 + 6$ | | A1 | oe eg $y = (x - \frac{5}{2})^2 + \frac{31}{4}$ or $y = x^2 - 5x + 14$ oe |
| | | | | | | Total 4 marks |

| | | T T | | | |
|------------|--|-----------------------|---|------------|--|
| 22 | $x^{2} + (x+2)^{2} - 2(x+2) = 24$ | | 5 | M1 | for substituting linear equation into the |
| | | | | | quadratic equation |
| | $2x^2 + 2x - 24$ (=0) or $x^2 + x - 12$ (=0) | | | A 1 | for a correct equation in the form |
| | or $2x^2 + 2x = 24$ or $x^2 + x = 12$ | | | | $ax^2 + bx + c = 0$ or $ax^2 + bx = -c$ |
| | (x+4)(x-3) (=0) or | | | M1ft | dep on M1 for solving their quadratic equation |
| | $1 + \sqrt{1^2 - (4 \times 1 \times -12)}$ | | | | using any correct method (allow one sign error |
| | $x = \frac{-1 \pm \sqrt{1^2 - (4 \times 1 \times -12)}}{2 \times 1}$ or | | | | and some simplification – allow as far as |
| | | | | | |
| | $\left(x-\frac{1}{2}\right)^2-\left(\frac{1}{2}\right)^2-12=0$ | | | | $\frac{-1\pm\sqrt{1+48}}{2}$) or if factorising, allow brackets |
| | (2) (2) | | | | which expanded give 2 out of 3 terms correct) |
| | x = -4 and x = 3 | | | A 1 | for both x values dep on M1 |
| | (-4, -2) and $(3, 5)$ | (-4, -2) and $(3, 5)$ | | A1 | for both solutions dep on M1 |
| Alternativ | ve mark scheme for 22 | | | | |
| | $(y-2)^2 + y^2 - 2y = 24$ | | 5 | M1 | for substituting linear equation into the |
| | | | | | quadratic equation |
| | $2y^2 - 6y - 20$ (=0) or $y^2 - 3y - 10$ (=0) | | | A1 | for a correct equation in the form |
| | $2y^2 - 6y = 20$ or $y^2 - 3y = 10$ | | | | $ay^2 + by + c = 0$ or $ay^2 + by = -c$ |
| | (y-5)(y+2) = 0 or | | | M1ft | dep on M1 for solving their quadratic equation |
| | $2 + \sqrt{(2)^2 + (4 + 1 + 10)}$ | | | | using any correct method (allow one sign error |
| | $y = \frac{-3 \pm \sqrt{(-3)^2 - (4 \times 1 \times -10)}}{2 \times 1}$ or | | | | and some simplification – allow as far as |
| | 2 1 | | | | $3 + \sqrt{9 + 40}$ |
| | $\left(y - \frac{3}{2}\right)^2 - \left(\frac{3}{2}\right)^2 - 10 = 0$ | | | | $\frac{3\pm\sqrt{9+40}}{2}$) or if factorising, allow brackets |
| | $\begin{pmatrix} 2 \end{pmatrix} \begin{pmatrix} 2 \end{pmatrix}$ | | | | which expanded give 2 out of 3 terms correct |
| | y = 5 and y = -2 | | | A1 | for both y values dep on M1 |
| | (-4, -2) and $(3, 5)$ | (-4, -2) and $(3, 5)$ | | A1 | for both solutions dep on M1 |
| | | , , , , , , , | | | Total 5 marks |
| | | | | | |

| 23 | $\overrightarrow{PM} = -\frac{3}{2}\mathbf{a} - \frac{3}{4}\mathbf{b} + 4\mathbf{a} + \frac{1}{2}(2\mathbf{b} - 4\mathbf{a}) \left(= \frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b} \right)$ $\overrightarrow{AM} = 4\mathbf{a} + \frac{1}{2}(2\mathbf{b} - 4\mathbf{a}) (= 2\mathbf{a} + \mathbf{b})$ $\overrightarrow{AM} = 2\mathbf{b} + \frac{1}{2}(4\mathbf{a} - 2\mathbf{b}) (= 2\mathbf{a} + \mathbf{b})$ $\overrightarrow{MA} = \frac{1}{2}(2\mathbf{b} - 4\mathbf{a}) - 2\mathbf{b} (= -2\mathbf{a} - \mathbf{b})$ $\overrightarrow{MA} = \frac{1}{2}(4\mathbf{a} - 2\mathbf{b}) - 4\mathbf{a} (= -2\mathbf{a} - \mathbf{b})$ | | 3 | M1 | for finding \overrightarrow{PM} or \overrightarrow{AM} or \overrightarrow{MA} |
|----|---|-----|---|----|---|
| | $(AP:PM =) \begin{vmatrix} \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b} \end{vmatrix} : \begin{vmatrix} \frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b} \end{vmatrix} \text{ oe}$ $(AP:AM =) \begin{vmatrix} \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b} \end{vmatrix} : 2\mathbf{a} + \mathbf{b} (= 3:4) \text{ oe}$ $(AM:PM =) 2\mathbf{a} + \mathbf{b} : \left \frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b} \right (= 4:1) \text{ oe}$ $AP = 3PM \text{ oe eg } \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b} = 3(\frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b}) \text{ oe}$ $AM = \frac{4}{3}AP \text{ oe}$ $AM = 4PM \text{ oe}$ | | | M1 | For use of a correct ratio or fraction linking AP and PM or AP and AM or AM and PM (in either order) vectors must be in form pa + qb |
| | | 3:1 | | A1 | Total 3 marks |
| | 1 | | | l | 10th 5 littlins |

| 24 | $\frac{4(2x-3)-3(2x-5)}{(2x-5)(2x-3)} \text{ or } \frac{8x-12-6x+15}{(2x-5)(2x-3)} \text{ oe}$ | | 4 | M1 | Writing 1st fraction as a fraction over a common denominator (can be 2 separate fractions) |
|----|--|------------------------------|---|----|--|
| | x(3-2x)(3+2x) or $(3x-1)(2x-5)$ | | | M1 | Complete factorisation of numerator or denominator of 2nd fraction |
| | $\frac{2x+3}{(2x-5)(2x-3)} \times \frac{(3x-1)(2x-5)}{x(3-2x)(3+2x)}$ | | | M1 | may be partially simplified |
| | | $\frac{3x-1}{x(2x-3)(3-2x)}$ | | A1 | e.g. $\frac{3x-1}{x(2x-3)(3-2x)} \text{ or } $ $\frac{1-3x}{x(2x-3)^2} \text{ or } $ $\frac{3x-1}{x(12x-9-4x^2)} \text{ or } $ $\frac{3x-1}{(12x^2-9x-4x^3)} \text{ oe } $ isw for incorrect denominator expansion |
| | | | | | Total 4 marks |

| 25 | n = 50 | | 3 | B1 |
|----|---|----|---|---|
| | $33125 = \frac{50}{2} [2 \times 50 + (50 - 1) \times k] \text{ oe}$ $33125 = 25 [100 + 49k] \text{ oe}$ $1325 = 100 + 49k \text{ oe}$ $1225 = 49k \text{ oe}$ | | | M1 For correct equation, using formula with $a = 50$ and $n = 50$ substituted (for this mark, allow $n = 49$) (k may be written as d) |
| | | 25 | | A1 |
| | | | | Total 3 marks |

| 26 | $1600 = \frac{1}{3} \times \pi \times r^2 \times 25 \text{ oe}$ | | 6 M1 | for substituting into volume formula for cone correctly and equating to 1600 |
|----|---|------|------|--|
| | $eg \ r = \sqrt{\frac{1600}{\frac{1}{3}\pi \times 25}} or$ | | M1 | dep for correct rearrangement of volume formula for r |
| | $r = \sqrt{\frac{192}{\pi}} (= \sqrt{61.1(154)} = 7.8176)$ | | | |
| | $l = \sqrt{"7.817"^2 + 25^2} (= \sqrt{686.1154} = 26.193)$ | | M1 | Dep on M2 correct method to find slant height of cone (radius of sector) |
| | $2 \times \pi \times \text{``7.817''} (= 49.1196)$ | | M | for using $C = 2\pi r$ oe using figures from correct method |
| | or | | | or |
| | $\pi \times "7.817" \times "26.193" (= 643.315)$ | | | for using $A = \pi r l$ using figures from correct method |
| | "49.1196" = $2 \times \pi \times$ "26.193" $\times \frac{x}{360}$ | | M1 | for using arc length = $2\pi r \times \frac{x}{360}$ |
| | or | | | or |
| | $ 643.315 = \pi \times 26.193 ^2 \times \frac{x}{360}$ | | | for using area of sector = |
| | 360 | | | $\pi r^2 \times \frac{x}{360}$ |
| | | 107° | A1 | for 107° - 108° |
| | | | | Total 6 marks |